# THE GREAT BOOK OF NUMBER MATHEMATICS GRADE 6



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## **NUMBER THEORY**



#### Exercise 1:

Write each number in figures.

(a) Weight

Thirty-five thousand, four hundred kilograms

(c) Time

Fifty thousand, six hundred and seventy-six hours

(b) Price

Forty thousand, four hundred and fifty Dollars

(d) Distance

**Eighty-nine thousand and seven kilometer** 

#### (e) Wiring

One million, seven hundred and seventy thousand meters

#### (f) Time

Seventy-four thousand, nine hundred years

#### Exercise 2:

Write each number in words.

- (a) 37,056
- (b) 1,400,334
- (c)400,004
- (d) 4,056,030
- (e) 13,000,003

#### Exercise 3:

What is the value of the red digit in each number?

- (a) 57,4300
- (b) 86,395
- (c)3,594,768
- (d) 8,834,950
- (e)379273402

#### Exercise 4:

Write the next 3 numbers in the sequence

(a)10,000 20,000 30,000 40,000 ...... (b)130,000 120,000 110,000 ...... (c)600,000 700,000 800,000 ...... (d)495,000 595,000 695,000 795,000 ....... (e)294,000 395,000 496,000 ......

## NUMBER THEORY: PRIME FACTORIZING

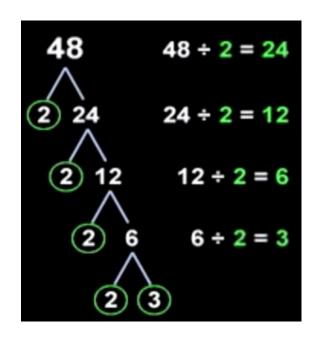
Factors are the number you multiply to get another

$$2 \times 6 = 12$$
Factors
Factors

Prime Numbers are those that can be divided by 1 or

Ex: 2, 3, 5, 7, 11, 17, 19, 23.....

Prime Factorization is finding which prime factors which multiply together to form the original number.



Start working with smallest prime number.

In this case 2

Continue dividing till the last 2 numbers are prime numbers

In this case 2 and 3

You can write the answer as

## Exercise 1:

List the prime factorization for each number

NUMBER	FACTORIZATION
24	
16	
14	
54	
27	
41	
31	
44	
44 63 58 30	
58	
30	

## **Greatest Common Factor**

#### Example:

Work out the greatest common factor of the following numbers:

12 AND 30

Factors of 12: 1,2,3,4,6,12

Factors of 30: 1, 2, 3, 5, 6, 10, 15, 30

The common factors are 1, 2, 3, 4, 6

Therefore 6 is the Greatest Common Factor

#### Exercise 1:

Find the GCF of the following numbers:

- 1) 12 and 24
- 2) 11 and 22
- 3) 18 and 21
- 4) 24 and 28
- 5) 64 and 54
- 6) 26 and 98
- 7) 32 and 72
- 8) 65 and 100
- 9) 144 and 156
- 10) 121 and 220
- 11) 156 and 299

## Least Common Multiple



This is simply the smallest positive number that is a multiple of two or more numbers.

For example:

Find the L.C.M of 60 and 12

Multiples of 60:

60,120,180,240,300

Multiples of 12:

12, 24, 36, 48, 60, 72

Therefore the least common multiple is 60

Find the Least Common Multiple for each number pair

- 1) 56,8
- 2) 30,9
- 3) 40,20
- 4) 48,8
- 5) 6,5
- 6) 8,24
- 7) 90,30
- 8) 24,12
- 9) 18,12
- 10) 5, 35
- 11) 72,48
- 12) 120,60,12

```
13) 30,40,50
```

## NUMBER THEORY: COMPOSITE NUMBERS OR PRIME NUMBERS

31 is a *prime*number because it
has exactly 2
factors: 1 and 31.

$$1 \times 31 = 31$$

32 is a composite number because it has more than 2 factors.

$$1 \times 32 = 32$$
  
 $2 \times 16 = 32$   
 $4 \times 8 = 32$ 

Factors are the number you multiply to get another number

#### Complete the table

Number List of factors Prime or Composite?

10	
5	
12	
18	
21	
36	
3	
79	
41	
31	
91	
77	
74	
51	

## **REVIEW- ADD AND SUBTRACT WHOLE NUMBER**

(1)



"Can you help me find the amount of fishes I caught?"

(1) Find the total number of each type of fish

ln t	he bay	In the
cavern		
(a) Jets	631	
278		
(b) Amberjack	5447	
3649		

- (2) How many more of each type of fish are in the bay than in the Carven?
- (3) Copy and complete

1764

- 2485

1392

(4) Find the number of fishes at each location

(a) Bay:

(5) Altogether there are 5000 fish. Half of them are blue. The rest are black or red. There are 100 more black fish than red fish. How many of each color fish are there?



(6) Mr. Jack has to put his money in the banks below. Each bank shows the number of money in it.

I need help in managing my accounts in the banks.









Mr. Jack tries this:

Bank A: \$6371

Bank C: \$6342 Bank D: \$8256

(a) How much more money could Mr. Jack put in

Bank A Bank C Bank D

- (b) How much money could possibly by all of the banks combined together?
- (c) Mr. Jack has \$15000, how can he distribute this amoung his banks? List 1 possible way.

## Multiplication



I have suddenly just forgot my passcode to enter my secret layer. I have 4 security buttons on my door to enter my layer. Could you

(1) (a) The total of the products in each button the codes to his secret layer

9 X 7	13 X 18	
10 x11	23 X 25	
7 X 5	4 X 40	
12 X13	9 X 60	
64 X 4	56 X 18	
36 X 13	1552 X 3	
16 X 6	93 X 8	
47 X 4	106 X 7	
64 X 4 36 X 13 16 X 6	56 X 18 1552 X 3 93 X 8	

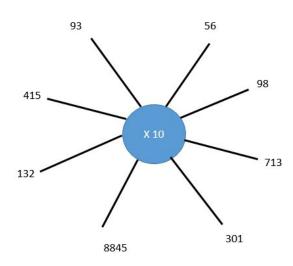
(1) (b) Batman crosses the security mat by stepping only on the rectangels which have an even product.

Which rectangles can he step on?

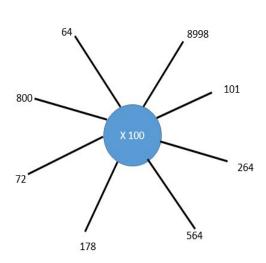
4 X 50	76 X 3	46 X 6	32 X8
17 X 15	11 X 16	23 X 7	15 X 6
34 x 5	6814 x 1	46 x 4	26 x 7
90 x 2	45 x 5	56 x 2	18 x 5

### (2) Multiply the following:

(a)



(b)



#### Multiplication of more than 2 numbers

For Example:

2 X 3 X 4

Multiply from right to left

= 6 X 4 the left Continue multiplying form the right to

2.4

- (3)
- (a) 2 X 3 X 6
- (b) 8 X 5 X 2
- (c) 1 X 19 X 10
- (d) 2 X 3 X 9
- (e) 10 X 14 X 3
- (f) 32 X 1 X2
- (4)
- (a) 2 X 76 X 5
- (b) 86 X 12 X 10

- (c) 2 X 53 X 2
- (d) 6 X 21 X 13
- (e) 12 X 3 X 12
- (f) 56 X 2 X 5
- (5) There are loads of supply on trucks, vans and planes.

Find the number of items unloaded on each transportation vehichle

- (a) 4 trucks 2541 crates on each
- (b) 2 vans -- 898 boxes on each
- (c) 5 planes 9045 packages on each
- (d) 3 Lorries 3901 packs on each
- (6) Find how many boxes of medicine were unloaded on each convoy of trucks

	Number of trucks in convoy	Medicine boxes on each truck
(a)	6	3715
(b)	4	2098
(c)	5	6327
(d)	2	10457

- (7) Solve the following
- (a) 3120
- (b) 4023
- (c) 5634
- (d) 5730
- (e) 2098

<u>X 4</u>

<u>X 7</u>

<u>X 5</u>

<u>X 6</u>

<u>X 8</u>

- (g) 167
- (h) 1670
- (j) 2000
- (h) 1320
- (i) 4883
- (j) 5601
- (k) 7429

<u>X14</u>

<u>X 10</u>

<u>X 13</u>

<u>X 12</u>

X 18

X 23

X

26

## Divisibility Rules

## Is the rule to test if one number is divisible by another

Divisible By:	Rules:	Example:
2	If the last digit is even	64 YES
	(0,2,4,6,8)	65 <b>NO</b>
3	The sum of the digits of	255 (2 +5 +5 = 12 and 12
	the number is divisible by 3	/3 = 4) <b>YES</b>
		316 (3 + 1 +6 = 10, and 10/
		3 =3 1/3) <b>No</b>
4	The Last 2 digits are	1012 is (12 / 4) = 3 <b>Yes</b>
	divisible by 4	5019 is not
5	The last digit is 0 or 5	165 <b>Yes</b>
		409 <b>No</b>
6	The number is divisible by	114 (it is even, and
	both 2 and 3	1+1+4=6 and 6÷3 = 2) <b>Yes</b>
		308 (it is even, but
		3+0+8=11 and 11÷3 =
		3 2/3) <b>No</b>
7	If you double the last digit and subtract it from the rest of the	343 (Double 3 is 6, 34-6=28, and 343÷7=49) <b>Yes</b>
	number and the answer	905 (Double 5 is 10, 90-
	is:	10=80, and 80÷7=11 3/7)
	• 0, or	No
	divisible by 7	100016 (016 0 100)
8	Last three digits are	109816 (816÷8=102) Yes
	divisible by 8	216302 (302÷8=37 <sup>3</sup> / <sub>4</sub> ) <b>No</b>
9	Sum of the digits is divisible by 9	1629 (1+6+2+9=18, and again, 1+8=9) <b>Yes</b>

		2013 (2+0+1+3=6) <b>No</b>
10	The number ends in 0	530 <b>Yes</b>
		531 <b>No</b>
11	If you sum every second digit and then subtract all other digits and the answer	1364 ((3+4) - (1+6) = <b>0</b> ) Yes
	is:	25176 ((5+7) - (2+1+6) = 3) No
	• 0, or	3) 110
	divisible by 11	

## Division

- 1. Help distribute the items of medicine. Find out how many sets are there and how many items are items are left over?
  - (a) 17 crutches of in sets of 2
- (c) 48 slings in sets of 6
- (b) 36 sticks in sets of 5
- (d) 108 bandages in sets of 12
- 2. Solve the following and include the remainder if necessary
  - (a) 30/2
  - (b) 60/5
  - (c) 29/3
  - (d) 23/6
  - (e) 39/4
  - (f) 36/7
  - (g) 1/3 of 24
  - (h) 1/4 of 28
  - (i) ½ of 20
  - (j) 1/5 of 25
  - (k) 1/6 of 36
  - (l)  $61 \div 6$
  - (m)  $84 \div 5$
  - (n) 93 ÷ 7
  - (o)  $101 \div 4$
  - $(p) 57 \div 6$

#### Example:

Nick shares 527 packets of cotton wool

5<sup>2</sup>2<sup>1</sup>7

Equally among 3 boxes

Each box has 175 packets. There are 2 packets left over.

- 3. Share equally. How many are in each box and how many are left over?
- (a) 467 tubes in 2 boxes
- (c) 801 spoons in 4 boxes
- (b) 863 toothbrushes in 3 boxes
- (d) 658 in 5 boxes
- 4. Solve the following
- (a) 305/4
- (b) 786/8
- (c) 193/2
- (d) 369/7
- (e) 1023/5
- (f) 2498/13

#### Example:

Nick puts gems into sets of 10. Look at these division

- 5. Solve the following
- (a) 2813 ÷ 10
- (b) 6500 ÷ 10
- (c) 506 ÷ 10
- (d) 6152 ÷ 10
- (e) 7491 ÷ 10
- (f) 1/10 of 8084
- (g) 6931 ÷ 10
- (h) 1/10 of 2040
- (i) 6684 ÷ 6
- $(j) 7982 \div 3$

- (k) 1465 ÷ 7 (l) 4250 ÷ 6
- (m) 4712 ÷ 19
- (n) 19,716 ÷ 12
- (o) 1/7 of 3451
- (p) 1/6 of 2946
- (q) 1/6 of 7152
- (r) 1/7 of 2674
- 6. Nick collects a rewards of \$ 1 for every 10 grams she finds. How much is her reward for finding all of these gems?

2278
Diamonds

3429
Rubies

- 7. Nick finds a box containing 1326 beads for bracelets. How many bracelets can be made, with 7 beads?
- 8. A set of 6 silver trays is worth \$ 3846. What is the value of each tray?
- 9. Nick finds that 1 gold chain weighs same as 2 silver chains. 3 gold chains and 1 silver chain weigh 1162 grams. What is the weight of each kind of chain?
- 10. Driver 'X' crashed a car. The repairs cost \$ 1248. Nick has to pay one eighth of the bill. How much does Driver 'X' have to pay?

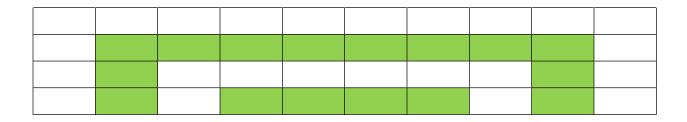
## Percentages

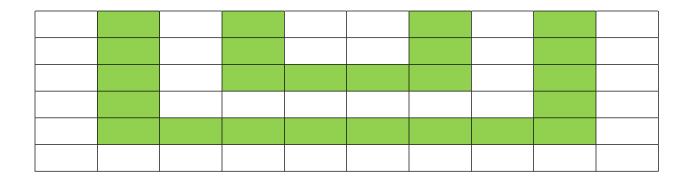
Percentage Concept

"In this floor design 40 of 100 tiles are red"

40 out of 100 = 
$$\frac{40}{100}$$
 = 40 per cent

40 per cent can be written as 40%

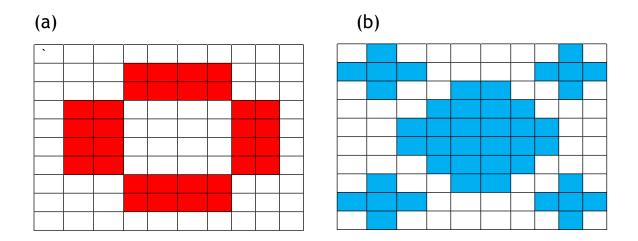




(1) For each of these floor designs, copy and complete

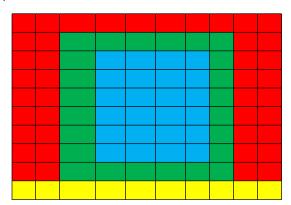
 $\frac{100}{100}$  or % is colored

 $\overline{_{100}}$  or % is **NOT** colored

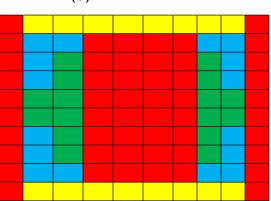


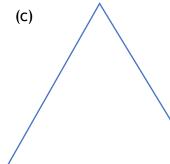
- 2. For each of table below, find the percentage colored
  - Blue
  - Red
  - Green
  - Yellow

(a)



(b)





centage of quantity

$$50\% = \frac{1}{2}$$

**25**% = 
$$\frac{1}{4}$$

**75**% = 
$$\frac{3}{4}$$

10% = 
$$\frac{1}{10}$$

There are 30 fruits in a bag. 30% of them are apples.

$$30\% = \frac{3}{10}$$

30 % of 30

$$=\frac{3}{10}$$
 of 30

=9

There are 9 apples in the bag



- (1) Find
- (a) 25% of 16

- (b) 25% of 8
- (c) 25% of 100
- (d) 50% of 50
- (e) 50% of 18
- (f) 50% of 12
- (g) 75% of 60
- (h) 75% of 90
- (i) 75% of 25
- (j) 10% of 5
- (k) 10% of 70
- (l) 10% of 16
- (2) Solve the following percentage quantities
- (a) 15% of 24
- (b) 65% of 45
- (c) 24% of 48
- (d) 100% of 1
- (e) 78% of 39
- (f) 55% of 60
- (g) 45% of 80
- (h) 60% of 40
- (i) 30% of 90
- (j) 10% of 180
- (k) 15% of 80
- (3) On each plane, 25% of the passengers are children. How many passengers on each plane are
  - (a) Children (b) Adults?



(4) Which How



train has more passengers who are Children? many more?

50%
Children

480
Passengers
Passengers

(5) The table displays the number of visitors this weekend.

Number of Visitors

Sat

580

Sun

300

Fri

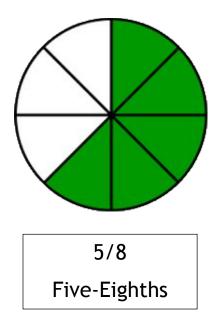
250

- 15% of these visitors were given a free chocolate
- 25% of these visitors were given a free pen
- 60% of these visitors were given a free poster

On each day of the weekend, how many were given free

(a) Chocolate (b) Pen (c) Poster

Fractions			
1/2	1/4	3/4	
One-Half	One-Quarter	One-Quarter	

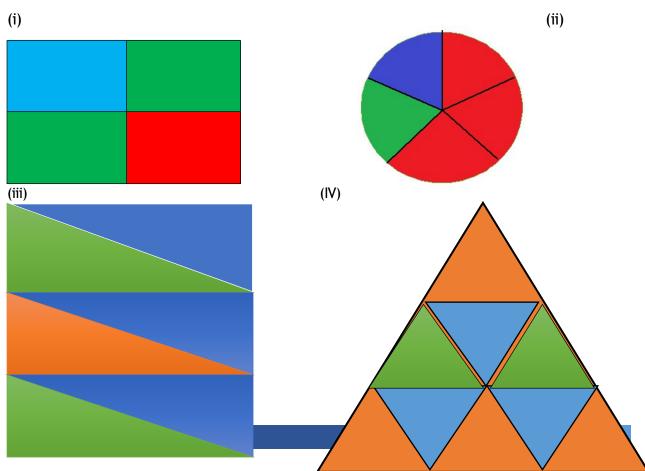


The top number tells how much section have been colored The bottom identifies the total number of sections

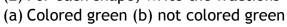
(1)

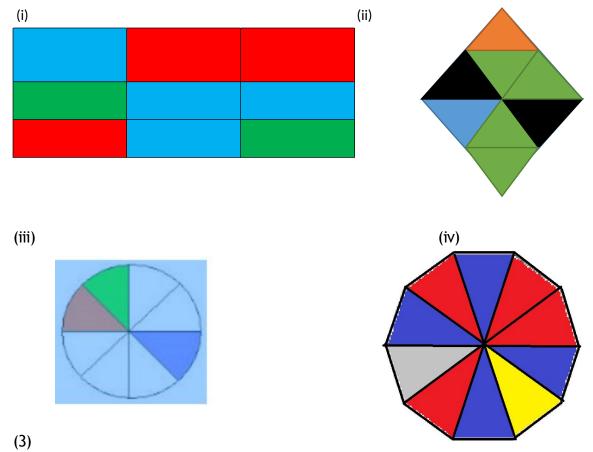
For each of the shapes below write the fraction colored:

(a) Blue (b) Green (c) Red

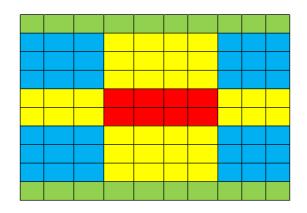








In this window there are different colors. Find the following fractions of colors given: (a) Green (b) Blue (c) Red (d) Yellow



## **Equivalent Fractions**

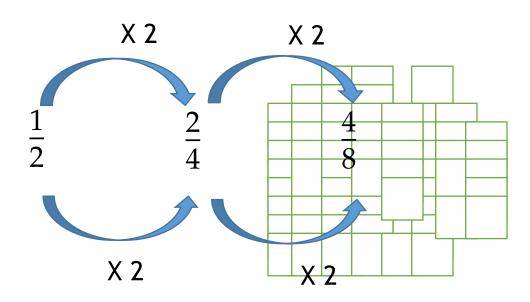
The Fractions below are all the same:

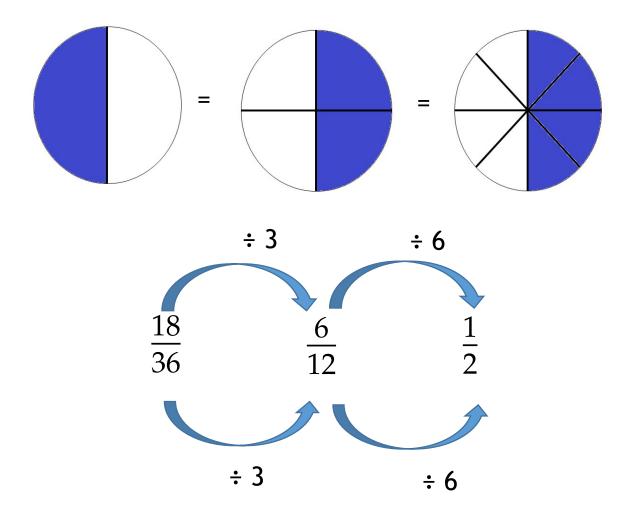
$$\frac{4}{8} = \frac{2}{4} = \frac{1}{2}$$

These fractions are the same.

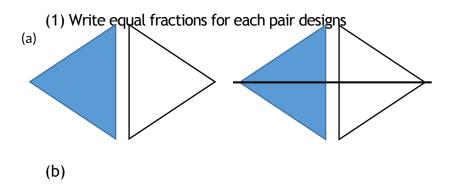
This is because when you multiply or divide both the top and bottom by the same number, the fraction keeps its value.

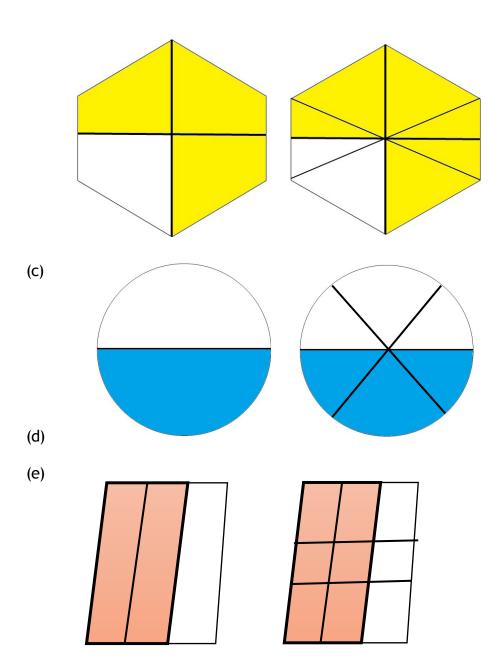
Rule: Change the denominator (bottom) using multiplication or division. And the same will be applied to the numerator (top).

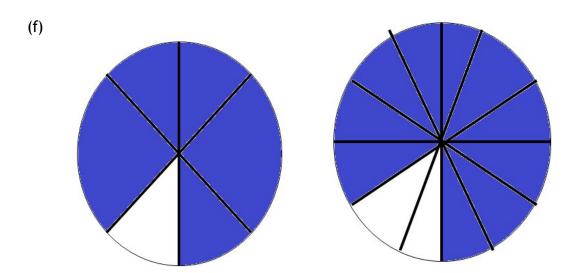




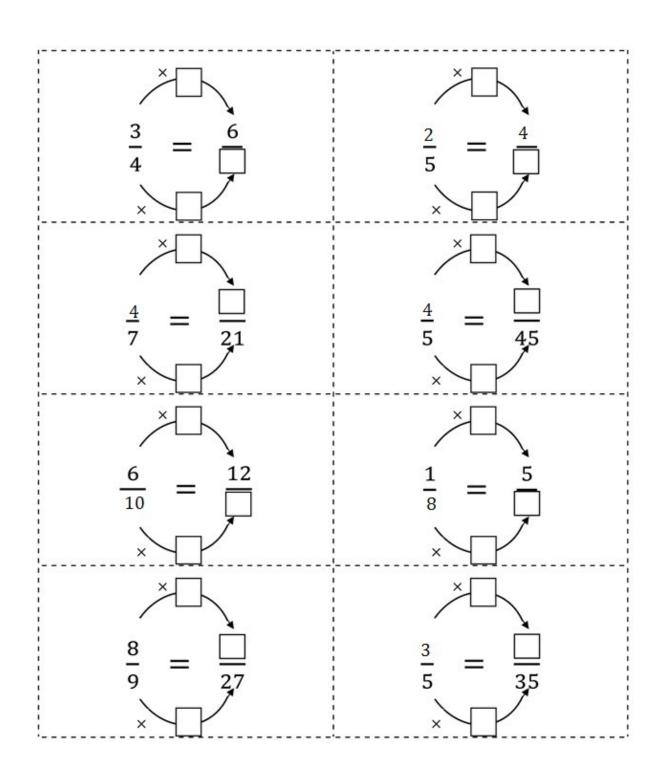
Choose a divisor, which creates results that are whole numbers. As you will divide further you reach an simplified fraction. In this case it is  $\frac{1}{2}$ .



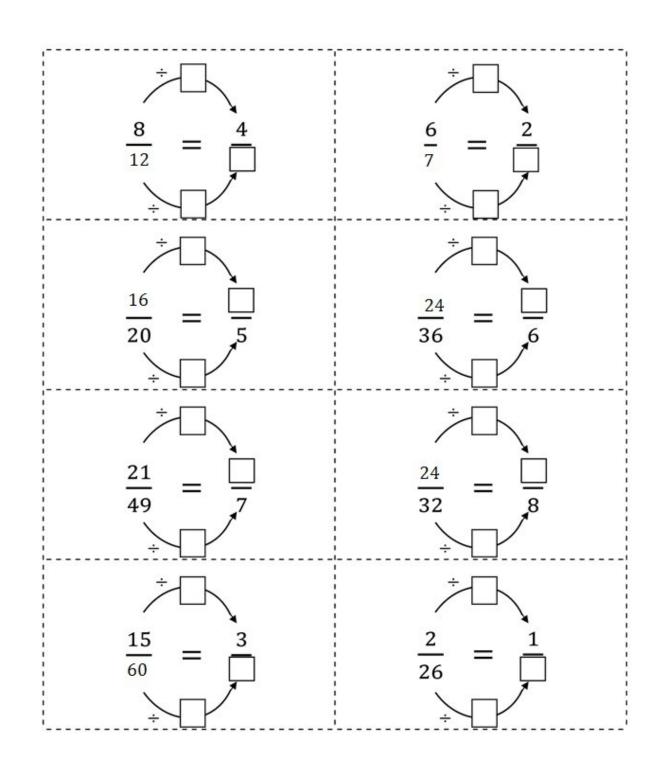




(2) Solve the following



(3) Solve the following



## Addition and subtraction of Fractions

Step 1: Ensure that the denominators are the same.

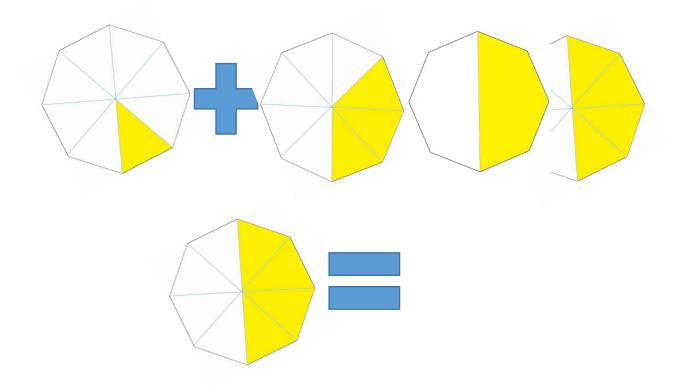
Step 2: Add the numerators, put the answer over the denominators.

Step 3: Simplify the fraction.

Step 1:  $\frac{1}{8} + \frac{3}{8}$ 

Step 2:  $\frac{1+3}{8} = \frac{4}{8}$ 

Step 3:  $\frac{4}{8} = \frac{1}{2}$ 



### Example 2:

Step 1: Ensure that the denominators are the same.

Step 2: Add the numerators, put the answer over the denominators.

Step 3: Simplify the fraction

## Solve the following sum

$$\frac{1}{3} + \frac{1}{6}$$



2+1\_3\_1

#### Example 3:

Solve the following sum

$$\frac{3}{5} + \frac{5}{15}$$

X 3

$$\frac{3 \times 3}{5 + \frac{5}{15}} = \frac{9 + 5}{15} = \frac{14}{15}$$

## Example 1:

Step 1: Ensure that the denominators are the same.

Step 2: Subtract the numerators, put the answer over the denominators.

Step 3: Simplify the fraction.

Step 1: 
$$\frac{1}{2} - \frac{1}{6}$$

Step 2: 
$$\frac{3}{6} - \frac{1}{6} = \frac{2}{6}$$



Example 2:

Step 1: 
$$\frac{2X_4}{5} \frac{1X_5}{4}$$
 X 5

Step 2: 
$$\frac{8+5}{20} = \frac{13}{20}$$

Step 3:

 $\frac{13}{20}$  Can not be futher simplified

(1) Solve the following:

$$\frac{2}{5} + \frac{3}{5} =$$

$$\frac{3}{6} - \frac{5}{9} =$$

$$\frac{3}{7} + \frac{3}{14} =$$

$$\frac{5}{12} - \frac{10}{12} =$$

$$\frac{11}{22} + \frac{10}{11} =$$

$$\frac{8}{24} - \frac{5}{12} =$$

$$\frac{28}{121} + \frac{72}{121} =$$

$$\frac{3}{7} - \frac{14}{42} =$$

$$\frac{7}{15} + \frac{4}{30} =$$

$$\frac{21}{101} - \frac{17}{101} =$$

$$\frac{10}{31} + \frac{15}{31} =$$

$$\frac{95}{161} - \frac{35}{161} =$$

- (2) Solve the following word problems
- (a) You give 1/3 of the flour to Susan and 1/6 of the wheat to Patrick. How much of the pan of brownies did you give away?

(b) Tim goes for a long a cycle ride. He cycles 3/4 km and then rest. Then he cycled 3/8 of a km. How far did he cycle altogether?



- (c) Nick walks 7/8 of a km to metro. Sam cycles 1/2 of a km to metro. How much farther does Nick walk than Sam?
- (d) Josh made two types of cakes. He used 2/3 cup of sugar for one recipe and 1/4 cup of sugar for the other. How much sugar did he use in all?

# Multiplication of fractions

Steps to multiply fractions

Step 1: Multiply the numerators

Step 2: Multiply the denominators.

Step 3: Simplify the fraction if needed.

### Example 1:

Solve 
$$\frac{3}{4} \times \frac{2}{3}$$

Step 1: 
$$\frac{3}{4} \times \frac{2}{3} = \frac{3 \times 2}{4 \times 3} = \frac{6}{12}$$

Step 2: 
$$\frac{6}{12} = \frac{1}{2}$$

Example 2:

Step 1: 
$$\frac{11}{5} \times \frac{6}{10} = \frac{11 \times 6}{5 \times 10} = \frac{66}{50}$$

Step 2:

 $\frac{66}{50}$  This can not be futther simplified

### Example 3:

Solve: 
$$\frac{3}{10} \times \frac{7}{9} \times \frac{3}{6} = \frac{3 \times 7 \times 3}{10 \times 9 \times 6} = \frac{63}{540}$$

(1) Find the value of each expression

Solve from left to right 
$$\frac{63}{540}$$
 This can be simplified

$$\frac{63}{540} \div \frac{9}{9} = 7/60$$

1. 
$$\frac{5}{6} \times \frac{1}{4}$$

5. 
$$\frac{8}{9} \times \frac{3}{2}$$

9. 
$$\frac{4}{9} \times \frac{7}{12}$$

2. 
$$\frac{4}{9} \times \frac{2}{3}$$

6. 
$$\frac{5}{11} \times \frac{1}{3}$$

10. 
$$\frac{7}{8} \times \frac{4}{6}$$

3. 
$$\frac{3}{5} \times \frac{3}{4}$$

7. 
$$\frac{11}{16} \times \frac{5}{6}$$

$$11.\frac{20}{24} \times \frac{5}{6}$$

4. 
$$\frac{5}{6} \times \frac{9}{11}$$

8. 
$$\frac{6}{13} \times \frac{22}{36}$$

$$\frac{19}{40} \times \frac{9}{19}$$

(2) Solve the following expressions

$$\frac{10}{15} \times \frac{3}{11} \times \frac{3}{9} =$$

$$\frac{8}{12} \times \frac{8}{18} \times \frac{5}{7} =$$

$$\frac{10}{17} \times \frac{12}{25} \times \frac{10}{13} =$$

$$\frac{8}{13} \times \frac{21}{27} \times \frac{10}{12} =$$

$$\frac{13}{20} \times \frac{16}{18} \times \frac{6}{10} =$$

$$\frac{15}{25} \times \frac{30}{40} \times \frac{10}{20} =$$

$$\frac{11}{15} \times \frac{10}{14} \times \frac{22}{27} =$$

$$\frac{8}{10} \times \frac{10}{15} \times \frac{3}{2} =$$

$$\frac{37}{40} \times \frac{10}{12} \times \frac{7}{13} =$$

$$\frac{16}{28} \times \frac{21}{24} \times \frac{4}{7} =$$

(3) Solve the following word problems and simplify all of your answers.

- (a) On Saturday, Nick ate pizza for dinner and had 1/2 of the pizza left over. On Sunday, he ate 1/3 of what was left. How much pizza did Nick eat on Monday?
- (b) In Tom's class, 2/3 of the pupils have a sister. Of the pupils who have a sister, 1/2 also have a brother. What fraction of the students in Tim's class have both a sister and a brother?
- (c) Ahmad runs an apple juice stand. On Sunday he used 6/8 of a bag of apples. On Monday he used 1/10 as many apples as on Sunday. How many bags of apples did Justin use on Monday?
- (d) Sam's cupcakes recipe calls for 1/2 of a cup of sugar. How much sugar would be used to make 1/4 of a batch of cupcakes?
- (e) The giraffe at the Al-Aim Zoo are fed 1/2 a barrel of corn each day. The elephant are fed 7/10 as much corn as the giraffe. How many barrels of corn are the elephant fed each day?
- (f) At a Arcade, 8/12 of the games are shooting games. Among the shooting games, 1/2 are first person games. What fraction of the games at the Arcade are first person games?
- (g) Of the students in the Harry's band, 1/2 play drum. Of the students who play a drum, 1/5 play the piano. What fraction of the students in the band play the paino?
- (h) Michael had 1/3 of a pie. He gave 3/4 of what she had to his friend Jason. What fraction of the whole pie did Jason get?

## Division of fractions

Step 1: Turn the second fraction (divisor) upside down, this called reciprocal.

Step: Multiply the first fraction the r reciprocal.

Step 3: Simplify the fraction

### Example:

$$\frac{1}{6}$$
 becomes  $\frac{6}{1}$ 

$$\frac{1}{2} \times \frac{6}{1} = \frac{1 \times 6}{2 \times 1} = \frac{6}{2}$$

$$\frac{6}{2}$$
 = 3

### Example:

Solve: 
$$\frac{4}{9} \div \frac{7}{12}$$

$$\frac{7}{12}$$
 becomes  $\frac{12}{7}$ 

$$\frac{4}{9} \times \frac{12}{7} = \frac{4 \times 12}{9 \times 7} = \frac{48}{63}$$

$$\frac{16}{21}$$
= 3

**(1)** Solve the following questions

1) 
$$\frac{1}{2} \div \frac{11}{20} =$$

6) 
$$\frac{17}{18} \div \frac{4}{8} =$$

1) 
$$\frac{1}{2} \div \frac{11}{20} = 6$$
)  $\frac{17}{18} \div \frac{4}{8} = 11$ )  $\frac{4}{8} \div \frac{3}{7} = 11$ 

2) 
$$\frac{6}{8} \div \frac{6}{7} =$$

7) 
$$\frac{6}{9} \div \frac{2}{4} =$$

2) 
$$\frac{6}{8} \div \frac{6}{7} = 7$$
)  $\frac{6}{9} \div \frac{2}{4} = 12$ )  $\frac{1}{2} \div \frac{6}{7} = 12$ 

3) 
$$\frac{1}{16} \div \frac{4}{14} =$$

8) 
$$\frac{3}{14} \div \frac{1}{10} =$$

3) 
$$\frac{1}{16} \div \frac{4}{14} = 8$$
)  $\frac{3}{14} \div \frac{1}{10} = \frac{3}{13}$ )  $\frac{3}{5} \div \frac{1}{3} = \frac{1}{3}$ 

4) 
$$\frac{1}{3} \div \frac{9}{20} =$$

9) 
$$\frac{2}{6} \div \frac{12}{14} =$$

4) 
$$\frac{1}{3} \div \frac{9}{20} = 9$$
)  $\frac{2}{6} \div \frac{12}{14} = 14$ )  $\frac{5}{10} \div \frac{1}{2} = 14$ 

5) 
$$\frac{10}{16} \div \frac{3}{9} =$$

$$0) \frac{9}{14} \div \frac{5}{10} =$$

5) 
$$\frac{10}{16} \div \frac{3}{9} = 10$$
)  $\frac{9}{14} \div \frac{5}{10} = 15$ )  $\frac{4}{6} \div \frac{12}{14} =$ 

(2) Solve the following equations:

1) 
$$\frac{6}{10} \div 10 =$$

11) 
$$\frac{1}{3} \div 4 =$$

2) 
$$\frac{1}{9} \div 13 =$$

12) 
$$\frac{2}{3}$$
 + 10 =

3) 
$$\frac{2}{3} \div 9 =$$

13) 
$$\frac{1}{2}$$
 + 2 =

4) 
$$4 \div \frac{2}{5} =$$

14) 
$$\frac{3}{9}$$
 + 14 =

5) 
$$\frac{6}{9} \div 8 =$$

15) 
$$\frac{5}{8}$$
 + 14 =

6) 
$$\frac{5}{8} \div 18 =$$

7) 
$$\frac{5}{6} \div 15 =$$

8) 
$$\frac{1}{7} \div 10 =$$

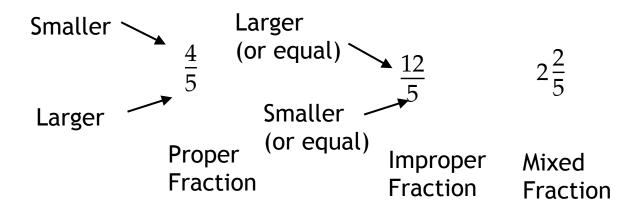
9) 
$$\frac{2}{5} \div 6 =$$

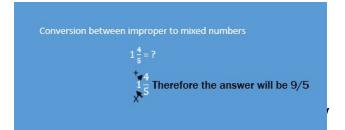
10) 
$$9 \div \frac{1}{8} =$$

- (3) Division world problems:
- (a) Jason has 2/4 of a pizza and he want to share it equally between 2 people. How much of the pizza does each person get?

- (b) Nicole is baking a cake. She uses 1/4 cup of oil for each cake. How many cakes can she make if she has a bottle of oil that has 6 cups in it?
- (c) How many 1/2 cup servings are in a package of salt that contains 5 1/4 cups altogether?
- (d) Mrs. Fabian is making pillow cases. Each pillow case uses 3/4 of a yard of fabric. How many pillow cases can she make out of 12 1/2 yards of fabric?
- (e) A closet is 3 1/2 feet long and a cube of ice is stored there. Each book on the cube is 5/8 inches wide. How many cubes will fit on the shelf?

## Improper and proper Fraction





To convert mixed fraction to an improper fraction

You must multiply the denominator with the whole number.

And then add it with the numerator.

To convert an improper fractions with a mixed fraction

You must divide the numerator by the denominator. Write down the whole number answer.

Then write down any remainder above the denominator.

Convert 7 into a mized number

$$\frac{7}{4} = ?$$

7 7 divided4 has a remainder of 3 Therefore the answer is 3

**(1)** Convert the following mix fractions into improper fractions:

1) 
$$5\frac{1}{4} =$$
 2)  $5\frac{9}{10} =$  3)  $2\frac{2}{9} =$ 

$$2) 5\frac{9}{10} =$$

3) 
$$2\frac{2}{9}$$
 =

4) 
$$4\frac{2}{5} =$$

5) 
$$9\frac{1}{2}$$
 =

4) 
$$4\frac{2}{5} =$$
 5)  $9\frac{1}{2} =$  6)  $2\frac{3}{4} =$ 

7) 
$$6\frac{6}{7}$$
 =

8) 
$$6\frac{3}{4}$$
 =

7) 
$$6\frac{6}{7} =$$
 8)  $6\frac{3}{4} =$  9)  $3\frac{5}{7} =$ 

10) 
$$9\frac{1}{6} =$$

11) 
$$2\frac{10}{11}$$
 =

10) 
$$9\frac{1}{6} =$$
 11)  $2\frac{10}{11} =$  12)  $6\frac{1}{3} =$ 

13) 
$$9\frac{4}{5} = 14) 8\frac{1}{2} = 15) 5\frac{1}{6} =$$

14) 
$$8\frac{1}{2}$$

15) 
$$5\frac{1}{6}$$
 =

(2) Convert the following improper fractions into mix fractions

1) 
$$\frac{39}{12}$$
 =

2) 
$$\frac{74}{10} = 3$$
 3)  $\frac{7}{2} =$ 

3) 
$$\frac{7}{2}$$
 =

4) 
$$\frac{33}{7}$$
 =

5) 
$$\frac{19}{3} = 6$$
 6)  $\frac{37}{10} =$ 

6) 
$$\frac{37}{10}$$
 =

7) 
$$\frac{23}{4} =$$

8) 
$$\frac{19}{3} = 9$$
 9)  $\frac{49}{9} =$ 

9) 
$$\frac{49}{9}$$
:

10) 
$$\frac{41}{6} =$$
 11)  $\frac{59}{11} =$  12)  $\frac{28}{6} =$ 

$$\frac{59}{11} =$$

12) 
$$\frac{28}{6}$$

13) 
$$\frac{31}{12}$$
 =

13) 
$$\frac{31}{12} =$$
 14)  $\frac{41}{8} =$  15)  $\frac{23}{5} =$ 

15) 
$$\frac{23}{5} =$$

## Conversion: Between Decimals and Fractions

Step 1: Write the decimal by 1

**Step 2:** Multiply both numerator and denominator by 10 for every decimal point.

Step 3: Simplify fraction

### Example 1:

Write 0.25 as afraction

Step 1: 
$$\frac{0.25}{1}$$

X 100

Step 2:  $\frac{0.23}{1} = \frac{25}{100} = \frac{1}{4}$  (2 decimal points therfore multiply by

100)

X 100

Step 3:  $\frac{25}{100} = \frac{1}{4}$  (Simplify)

### Example 2:

Write 5.7 as afraction

Step 1:  $\frac{5.7}{1}$ 

Step 2:  $\frac{5.7}{1} = 5\frac{7}{10}$  (Sperate the whol number and convert the fractiontherfore 5.7 will be 0.7)

Step 3:  $5\frac{7}{10}$  (Cannot be simplified)

(1) Convert the following decimal into fractions

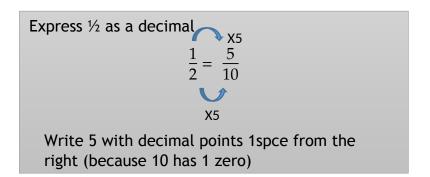
- (a) 0.9
- (b) 1.3
- (c) 0.4
- (d) 0.12
- (e) 0.75
- (f) 0.08
- (g) 6.4
- (h) 0.09
- (i) 5.9
- (j) 1.25
- (k) 6.5
- (l) 3.7
- (m) 4.3
- (n) 2.2
- (o) 2.15
- (p) 1.85
- (q) 5.55
- (r) 5.01
- (s) 0.777

## Convert Fractions into Decimals

**Step 1**: Find a number you can multiply by denominator of the fraction to make it 10, or 100, or 1000 etc.

**Step 2**: Multiply both the denominator and numerator by that number.

**Step 3**. Then write the numerator number, putting the decimal point in the correct spot.



1) 
$$\frac{3}{5}$$
 =

$$2) \frac{3}{4} =$$

$$3) \frac{2}{10} =$$

4) 
$$\frac{5}{6}$$
 =

$$5) \frac{1}{12} =$$

6) 
$$\frac{1}{12}$$
 =

$$7) \frac{4}{6} =$$

$$8) \frac{2}{3} =$$

9) 
$$\frac{2}{3}$$
 =

10) 
$$\frac{3}{4}$$
 =

# Decimals to Percentages and Vice Versa

To convert a decimal to a percentage you must multiply it by 100

To convert a percentage to a decimal you must move the decimal point 2 places to the left to remove the % sign.

Example 1:

Convert 1.2 to a percent

1.2 X 100 = 120%

Example 2:

Convert 58% to a percent

## Fractions to Percentages and Vice Versa

To convert percent to fraction

Step 1: Write the percent divided by 100

Step 2: If the percent is not a whole number multiply it by 10, 100 or 1000 to remove the decimal point.

Step 3: Simplify the fraction

### Example 1:

Convert 35 % to a decimal

 $\frac{35}{100} = \frac{7}{20}$  (divide both numerator and denominator by 5 to

### Example 2:

Convert 75.5% to a decimal

$$\frac{75.5}{1000} = \frac{755}{1000}$$

$$\frac{755}{1000} = \frac{151}{200}$$

To convert Fraction to a percent

Step 1: Divide the numerator by the denominator

Step 2: Multiply the result by 100

### Example 1:

Convert  $\frac{1}{4}$  as a percentage

$$\frac{1}{4} = \frac{25}{100} = 25\%$$

$$x = 25$$

$$x = 25$$

## Raviaw

Example 2:

Convert  $\frac{5}{16}$  as a percentage  $\frac{5}{16} = \frac{31.25}{100} = 31.25\%$ 

### Convert Decimal to Percent

$$0.62 =$$

$$0.92 =$$

$$0.42 =$$

$$0.317 =$$

### **Convert Percent to Decimal**

#### **Convert Decimal to Fraction**

$$0.17 =$$

$$0.35 =$$

### **Convert Fraction to Decimal**

$$\frac{48}{25} =$$

$$\frac{37}{40} =$$

$$\frac{8}{50} =$$

#### **Convert Fraction to Percent**

$$\frac{81}{50} =$$

$$\frac{34}{20} =$$

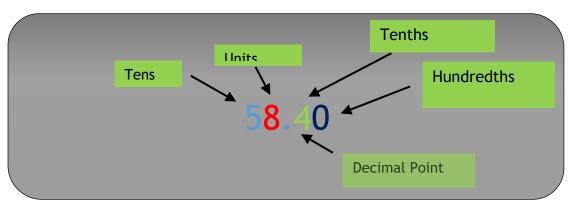
#### Convert Percent to Fraction

## **DECIMALS**

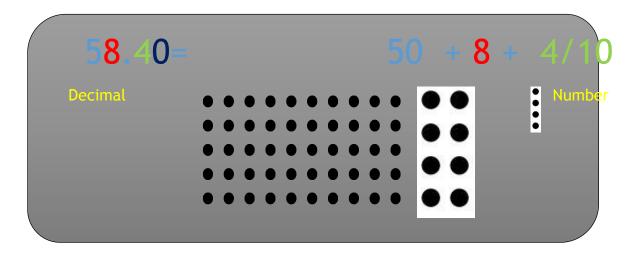
A fraction whose denominator is a power of ten and whose numerator is expressed by figures placed to the right of a decimal point.

### For Example:

"Fifty-eight and four tenths" can be written as a decimal number



### We can break this down



### The key to this is known as **PLACE VALUE**

Place Value can be described as the position or place of a number

## 836.47

The "6 "in this number is known as the unit

The "3 "in this number is known as the tens

The "8 "in this number is known as the hundred

The "4" in this number is known as tenths

The "7" in this number is known as hundredth





As the numbers move to the left they become 10 times bigger

For example thousands is 10 times bigger than hundred

**Opposites** 

As the numbers move to the right they become 10 times smaller

For example thousands is 10 times bigger than hundred

What happens after passing the "." (Decimal point)? Simple, follow the same pattern meaning 1/10 smaller



We call this eight hundred thirty-six and fourty-

write the following in digits:

1) Eight units and three tenths:

- 2) Seven units and eight tenths:
- 3) Four units and five thousandths:

- 4) Seven units and four hundredths:
- 5) Nine tens, five units, seven tenths and two hundredths:
- 6) Eights tens, eights units and three hundredths:
- 7) Five tenths, two hundredths and five thousandths:
- 8) Six units, three hundredths and three thousandths:
- 9) even units, six hundredths and five thousandths:

Write the following in word form:

- 1) 36.6
- 2) 92.8
- 3) 24.5
- 4) 59.6
- 5) 46.6
- 6) 42.1
- 7) 58.1
- 8) 41.2
- 9) 21.2
- 10) 45.2
- 11) 54.7
- 12) 56.9

Write the following in standard form:

- 1)20+6+0.9+0.06
- 2)30+1+0.7+0.07
- 3)40+9+0.2+0.06

- 4)30+7+0.6+0.07
- 5)30+5+0.8+0.01
- 6)50+7+0.4+0.04
- 7)50+2+0.4+0.06
- 8)70+8+0.3+0.07
- 9)20+1+0.3+0.02
- 10 ) 10 + 8 + 0.4 + 0.02
- 11)80+1+0.4+0.01
- 12)70+7+0.1+0.01
- 13 ) 40 + 1 + 0.1 + 0.04
- 14)40+2+0.9+0.09
- 15) 90 + 3 + 0.5 + 0.07

## Match the Number with the Correct Name

1) 4.72 A Seven

and Seven Tenths

2)	6.26	E	Seven and
Twelve	e Hundredths		
3)	2.71		Six and Twenty
Six Hur	ndredths		
4)	7.12		Nine and Twenty
Four H	undredths		
5)	9.85	E	Nine and
Fourte	en Hundredths		
6)	9.14	F	Nine and Eighty
Five Hu	undredths		
7)	4.72		G Two and Seventy
One Hu	undredths		
8)	9.24	H	H Five and Sixty
Eight H	lundredths		
9)	7.70	1	Four and Seventy
Two H	undredths		
10)	5.68	J	Four and Seventy
Two H	undredth		

## Addition and Subtraction of Decimals

#### Addition:

### **Explanation:**

To successfully add decimals numbers we have to ensure that the tens are added to tens, units to the units, and so forth. The numbers have to be written such that the 2 decimals points are aligned vertically. Add the zeros so that the numbers have the same length.

## Work Examples:

Note: The decimal point in the answer is vertically lined up with the decimal point in the number.

#### Subtraction:

#### **Explanation:**

To successfully subtract decimals numbers we have to follow the same steps but subtract the numbers.

\A/0 K	LVama	$\sim$
VVIII	K FXAIIII	
7 7 0 1	k Examp	$\cdot \cdot$

Work Example.		
8.005-2.6=	8.57 - 7.09 =	9.35 - 4.86 =
<sup>7</sup> .8.005	8 <sup>4</sup> <b>2</b> 7	8 <sup>12</sup> <b>2</b> . <b>2</b> 5
<u>-2.600</u>	<u>-7.09</u>	<u>-4.86</u>
5.405	1.48	4.49

### Evaluate the following:

b) 
$$81.92 + 9.26 =$$

c) 
$$82.36 + 82.36 =$$

d) 
$$1.63 + 3.44 =$$

e) 
$$6.5 + 1.23 =$$

f) 
$$88 + 9.09 =$$

g) 
$$57 + 46.45 =$$

b) 
$$0.89 + 0.73 =$$

c) 
$$5.06 + 1.78 =$$

### Getting a bit tricky

c) 
$$9 + 48.32 + 1.1 =$$

$$e) 86.2 + 36.95 =$$

g) 
$$3.1935 + 7 + 0.7 =$$

$$k) 0.2345 + 1.06 + 101 =$$

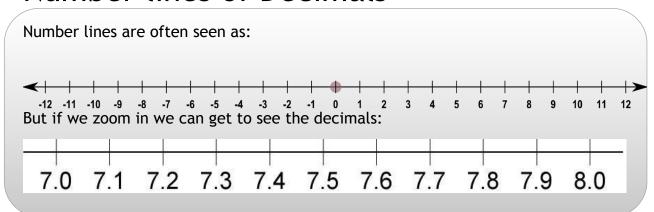
## Evaluate the following:

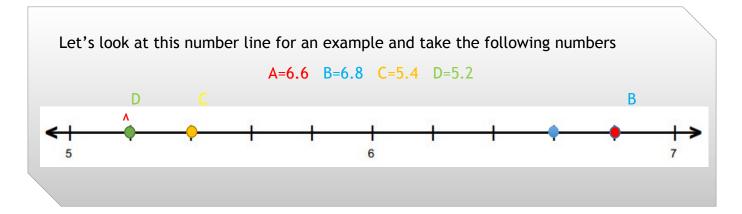
1:	2:	3:	4:	5:
0.45	0.32	0.28	0.76	0.18
- 8.20	- 0.14	- 0.96	- 0.29	- 0.59
6:	7:	8:	9:	10: 0.79
2.80	0.62	0.83	0.30	- 8.30
- 0.76	- 9.20	- 3.00	- 0.90	

11:	12:	13:	14:	15:
0.11	5.70	6.10	0.79	0.71
- 0.52 	- 0.13	- 0.70	- 0.61	- 7.70
16:	17:	18:	19:	20:
	0 47	0.45	0.52	0.43
0.20	0.47	0.45	0.52	0.12

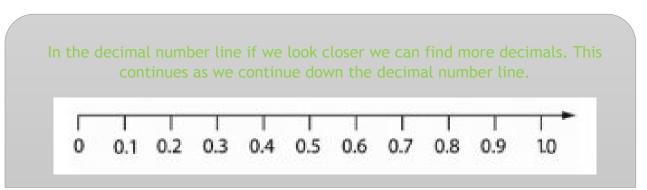
21:	22:	23:	24:	25:
4.60	0.24	0.93	0.95	6.20
- 0.52	- 1.20	- 0.15	- 7.90	- 0.46

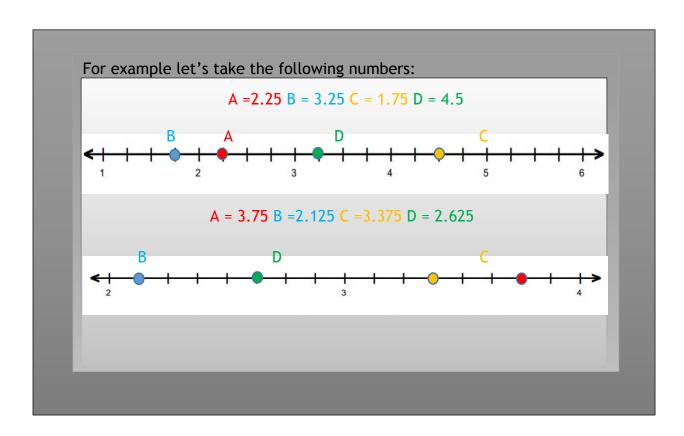
## Number lines of Decimals

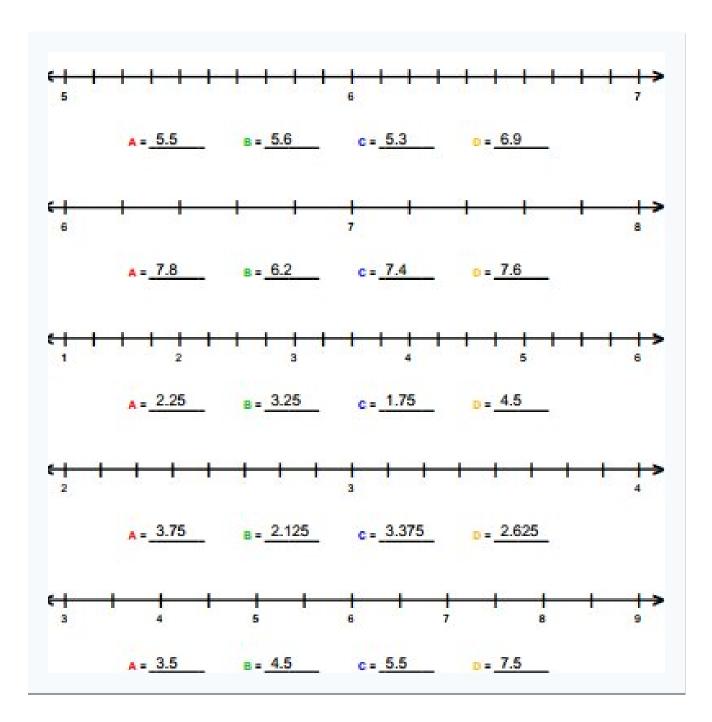


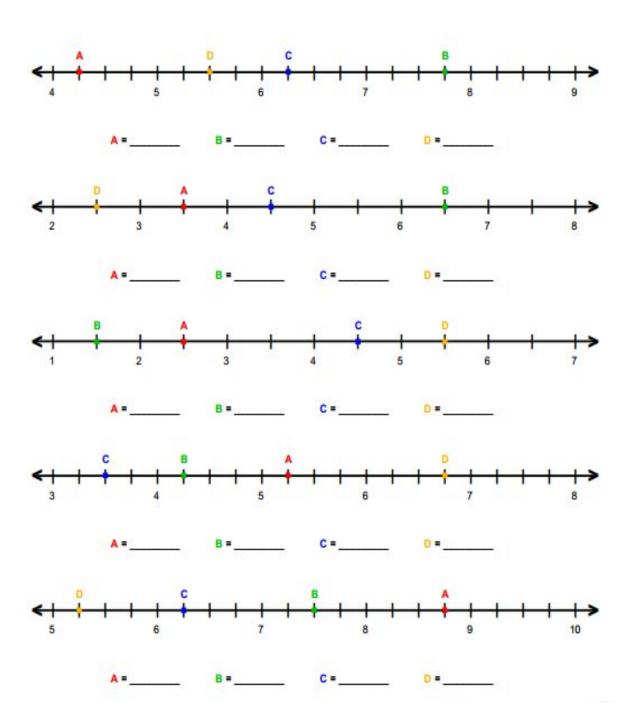


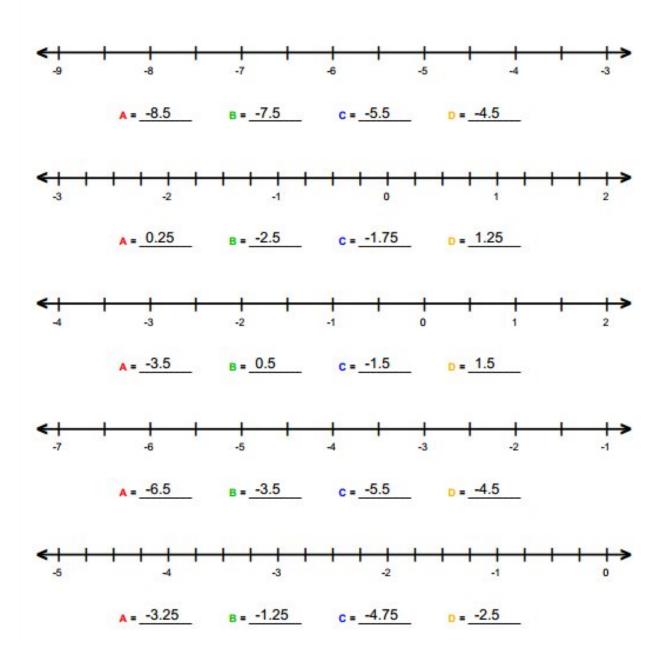
By looking closer we can find more decimals:











Multiplication of Decimals

### Multiplication:

### **Explanation:**

### To multiply decimals numbers you must follow these steps:

- Multiply the numbers normally, ignore the decimal point
- > Then put the decimal point in the answer it will have as many decimal places as the two original numbers

Note: The answer should have that many numbers after its decimals which can be counted up be how many numbers are after the decimal point in .both numbers you are multiplying.

### Work Examples:

Multiply 0.04 by 1.5

 $0.04 \times 1.5 =$ 

 $4 \times 15 = 60$  (multiply without the decimals)

0.04 has 2 decimals places

1.5 has 1 decimal places

i.e. the answer will have 3 decimal places 0.06

### Work Examples:

Multiply 0.5 by 9.5

 $0.5 \times 9.5 =$ 

5x 95 = 475 (multiply without the decimals)

0.5 has 1 decimals places

9.5 has 1 decimal places

i.e. the answer will have 2 decimal places 47.5

#### How does this all work?

When you multiplying without the decimal point, you are moving the decimal point to the right to get it out of the way:

Original:

1 Move:

2 Moves:

3 Moves:

 $0.04 \times 1.5 \implies 0.4 \times 1.5 \implies 4. \times 1.5$ 

 $4. \times 15.$ 

Then the multiplication:

$$4. \times 15. = 60.$$

But remember, we did 3 Moves of the decimal point, so we need to undo that:

3 Moves:

2 Moves:

1 Move:

Correct

55.

5.5

0.55

0.055

### Example 1

Multiply 0.75 by 34.5

 $0.75 \times 34.5 =$ 

75x345 = 25975 (multiply without the decimals)

0.75 has 1 decimals places

34.5 has 1 decimal places

i e the answer will have 2 decimal places

### Example 2

Multiply 0.78 by 105

 $0.78 \times 105 =$ 

78x105 = 8190 (multiply without the decimals)

0.78 has 2 decimals places

105 has decimal places

i e the answer will have 7 decimal places 81 9

## Solve the following:

1: 2: 4: 5: 
$$9.0 \times 7.1 \times 0.4 \times 0.4 \times 0.9 \times 1.8 \times 0.8 \times 0.8$$
6: 7: 9: 10:  $0.8 \times 0.8 \times 0.8$ 

1: 
$$6.5$$
 2:  $3:$  4:  $5:$   $4.0$   $\times 0.5$   $\times 0.5$   $\times 0.9$   $\times 1...9$   $\times 10.1$   $\times 1...9$ 

6:  $7:$  8:  $9:$  10:  $4.0$   $\times 1...$   $\times 1...$ 

1: 0.5 × 7.00	2: 7.8 × 8.9	3: 7 ×4.2	4:	7.3 × 8.0	5: 3.2 × 1.7
6: 20.0 × 2.6	7: 71.0 × 7.4	8: 37.0 × 7.4	9:	58.0 × 5.0	10: 89.0 × 5.4

## **Division of Decimals**

### Division:

## Explanation:

To divide decimals numbers you must follow these steps:

- Divide decimals numbers by ignoring the decimal point
- > Then put the decimal point in the same spot as the

#### Divide 9.1/0.4

Ignore the decimal point and do the division

30

<u>-28</u>

020

-20

00

### (1) Solve the following

2 a. 
$$8.8 \div 0.8 =$$

3 a. 
$$100.6 \div 22.2 =$$
 3 b.  $3.0 \div 0.3 =$ 

4 a. 
$$7.2 \div 1.6 =$$

5 a. 
$$93.9 \div 0.300 =$$

## (2) Solve the following